

## Planck 2018 results

### VI. Cosmological parameters (Corrigendum)

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In the original version, the bounds given in Eqs. (87a) and (87b) on the contribution to the early-time optical depth,  $\tau(15, 30)$ , contained a numerical error in deriving the 95th percentile from the Monte Carlo samples. The corrected 95% upper bounds are:

$$\begin{aligned}\tau(15, 30) &< 0.018 \quad (\text{lowE, flat } \tau(15, 30), \text{FlexKnot}); & (1) \\ \tau(15, 30) &< 0.023 \quad (\text{lowE, flat knot, FlexKnot}). & (2)\end{aligned}$$

These bounds are a factor of  $\sim 3$  larger than the originally reported results. Consequently, the new bounds do not significantly improve upon previous results from *Planck* data presented in Millea & Bouchet (2018) as was stated, but are instead comparable. Equations (1) and (2) give results that are now similar to those of Heinrich & Hu (2021), who used the same *Planck* 2018 data to derive a 95 % upper bound of 0.020 using the principal component analysis (PCA) model and uniform priors on the PCA mode amplitudes.

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